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Yacine Amirat, Vincent V. Choqueuse, Mohamed Benbouzid, Jean-Frederic Charpentier. Bearing Fault Detection in DFIG-Based Wind Turbines Using the First Intrinsic Mode Function. XIX International Conference on Electrical Machines (ICEM), 2010, Sep 2010, ROME, Italy. pp.1-6, 10.1109/ICELMACH.2010.5608066 . hal-01081638

**HAL Id: hal-01081638**

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Yacine AMIRAT, Vincent CHOQUEUSE, Mohamed BENBOUZID, Jean-Frederic CHARPENTIER  
- Bearing Fault Detection in DFIG-Based Wind Turbines Using the First Intrinsic Mode Function -  
In: XIX International Conference on Electrical Machines (ICEM), 2010, Italy, 2010-09 - Electrical  
Machines (ICEM), 2010 XIX International Conference on - 2010

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# Bearing Fault Detection in DFIG-Based Wind Turbines Using the First Intrinsic Mode Function

Y. Amirat, V. Choqueuse, M.E.H. Benbouzid and J.F. Charpentier

**Abstract**—Wind energy conversion systems have become a focal point in the research of renewable energy sources. In order to make the DFIG-based wind turbines so competitive as the classical electric power stations it is important to reduce the operational and maintenance costs by continuously monitoring the condition of these systems. This paper provides a method for bearing fault detection in DFIG-based wind turbines. The proposed method uses the first Intrinsic Mode Function (IMF) of the stator current signal. After extracting the first IMF, amplitude-demodulation is performed to reveal a generator bearing fault. Experimental results show that the proposed method significantly improves the result of classical amplitude-demodulation techniques for failure detection.

**Index Terms**—Wind turbine, Doubly Fed Induction Generator (DFIG), fault detection, bearings, signal processing

## I. INTRODUCTION

Wind energy conversion systems is the fastest-growing source of new electric generation in the world and it is expected to remain so for some time. In order to be more reliable and competitive than classical power generation systems and due to geographical location of DFIG-based wind turbines, it is important to prevent failure and to reduce maintenance cost. A deep knowledge about all the phenomena involved during the occurrence of a failure constitutes an essential background for the development of any failure diagnostic system. Regarding a failure as a particular input acting on the generator, a diagnostic system must be able to detect its occurrence, as well as to isolate it from all other inputs such as disturbances and controls affecting the behavior of the DFIG. For the failure detection problem, we would like to know if a failure exists or not in the Wind energy conversion system via the processing of available measurements.

A quantitative analysis of real wind turbine failure data has shown important features of failure rate values and trends [1]–[3]. A failures number distribution check-off is reported in Fig. 1 for Swedish wind power plants that occurred between 2000 and 2004 [3]. This figure shows that 45% of failures were linked to the electrical system, sensors and blades/pitch components. Experience feedback of wind turbine industries

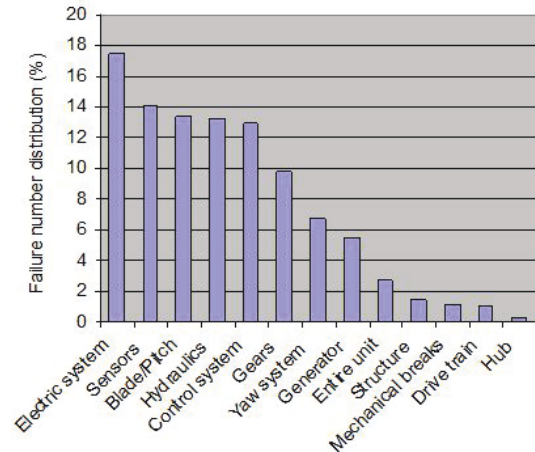


Fig. 1. Failures number distribution for Swedish wind power plants between 2000-2004 [3].

corroborates that the major concern is on the electrical system. Typical failures include:

- Generator bearing failure
- Dynamic air-gap irregularities
- Stator and rotor winding insulation failures.
- Inter-turn short circuits in stator windings
- Broken rotor bar or cracked rotor end-rings
- Harmonic derating

Many methods are available for condition monitoring of DFIG-based wind turbines. These include electrical quantities signature analysis (current, power,...), vibration monitoring, temperature monitoring and oil monitoring. In the case of DFIG-based wind turbines, it has been shown that failure in the drive train could be diagnosed from the electrical quantities of the generator. This principle has been used to diagnose unbalance and failure in the blades of a small wind turbine by measuring the power spectrum density at the turbine generator terminals [4]. The advantage of electrical signature analysis over other monitoring techniques is that the signals are easily accessible during operation i.e. the current can be acquired by current transformer, the voltage via a voltage transformer and the power by computation. Moreover, current and voltage transducers are usually cheaper than vibration and torque transducers. In this paper, the generator current is employed to detect faults in wind turbines. From a decision point of view, failure detection based on the current signal usually involves two steps: 1) a preprocessing step and a 2) failure detection

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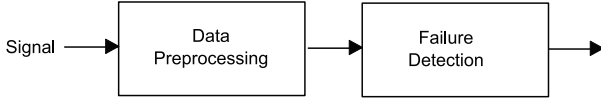


Fig. 2. Fault detection framework.

step (see Fig.2). The aim of the preprocessing step is to project the signal into a new space in order to facilitate the failure detection. In the literature, many preprocessing techniques have been proposed. These include the popular Fast Fourier Transform (FFT) [5], time-frequency representations [6]–[8], time-scale decompositions [9]–[11] and AM/FM demodulation techniques [12]–[16]. The major drawback of FFT and time-frequency representations is that they require the knowledge of the frequency components affected by the generator failure. Similarly, analysis based on wavelet decomposition usually requires the knowledge of the scale associated with the failure. Another commonly used method is the AM/FM demodulation technique. AM/FM demodulation technique is a well-suited tool for data preprocessing since most of the machine failure leads to current modulation [7], [8]. Under the assumption of a mono-component signal (i.e.  $x(n) = a(n)\cos(\phi(n))$ ), classical demodulation approaches are the Hilbert transform [13], [14] and the Teager energy operator [15], [16]. Unfortunately, in practice, both of these approaches are inappropriate as the mono-component assumption is rarely satisfied. To satisfy this assumption, band-pass filtering can be employed, however, it requires the knowledge of the central band-pass frequency and a proper filter design.

In this paper, we propose to use an Empirical Mode Decomposition (EMD) [17] to automatically extract a mono-component signal, called Intrinsic Mode Function (IMF), from the stator current signal. Then, we employ an Hilbert transform for AM demodulation. As opposed to the Hilbert-Huang transform which has been previously used for failure detection [18], [19], we propose to exploit only the first IMF since it contains most of the useful information. This paper is organized as follows. Section II presents the proposed approach and Section III reports on the experimental results.

## II. PREPROCESSING BASED ON THE FIRST IMF AND AM DEMODULATION

Let us denote by  $x(n)$  ( $n = 1, \dots, N$ ) the stator current signal. Under the multi-component assumption,  $x(n)$  can be decomposed as

$$x(n) = \sum_{k=1}^n \underbrace{a_k(n)\cos(\phi_k(n))}_{\text{IMF}_k(n)} + r(n) \quad (1)$$

where  $\text{IMF}_k(n)$  is the  $k^{\text{th}}$  Intrinsic Mode Function (IMF) and  $r(n)$  is the residue. In practice, the IMFs are unknown and must be extracted from the stator current signal  $x(n)$ .

### A. Extraction of the First IMF

The IMFs and the residue can be extracted from  $x(n)$  by using an Empirical Mode Decomposition (EMD) [17]. This

decomposition can be described as follows:

- 1) Identification of all extrema of  $x(n)$
- 2) Interpolation between minimal (resp. maxima) ending up with some envelope  $e_{\min}(n)$  (resp.  $e_{\max}(n)$ ).
- 3) computation of the mean:

$$r(n) = \frac{e_{\min}(n) + e_{\max}(n)}{2} \quad (2)$$

- 4) extraction of the detail:

$$\text{IMF}_k(n) = x(n) - r(n) \quad (3)$$

- 5) Iteration on the residue  $r(n)$ .

In practice, this algorithm has to be refined by a *shifting process* until the detail  $\text{IMF}_k(n)$  can be considered as an Intrinsic Mode Function [20]. In the following, we only decompose the stator current signal into one IMF and a residue ( $k = 1$ ) since this decomposition concentrates most of the useful information about the failure into one IMF. Increasing the number of components  $k$  tends to spread the information about the failure through several IMFs which can render interpretation more difficult.

Figures 3 to 6 present the current  $x(n)$ , the first IMF  $\text{IMF}_1(n)$  and the residue  $r(n)$  after one iteration of the EMD algorithm for healthy and faulty generators. For healthy generators (Figs. 3 and 5), one can notice that the first IMF is close to 0 and that the signal  $x(n)$  is close the residue  $r(n)$ . On the contrary, for faulty generators, Figs. 4 and 6 show that the first IMF is no longer equal to 0. This behavior can be observed for faulty generators with bearing inner race deterioration (Fig. 4) and with bearing ball deterioration (Fig. 6).

### B. Amplitude Demodulation

After applying the EMD, the first IMF is a mono-component signal which can be further processed with a classical demodulation tool. Indeed using (1), the first IMF,  $y(n)$ , can be expressed as

$$y(n) = \text{IMF}_1(n) = a_1(n)\cos(\phi_1(n)) \quad (4)$$

Under the assumption that a failure leads to stator amplitude modulation, most of the useful information is contained in the amplitude envelope  $|a_1(n)|$ . To extract  $|a_1(n)|$  from  $y(n)$ , we propose to use an amplitude demodulation technique based on the Discrete Hilbert transform (DHT). The DHT of  $y(n)$  is given by [21]

$$\mathcal{H}[y(n)] = \mathcal{F}^{-1} \{ \mathcal{F}\{y(n)\} \cdot u(n) \} \quad (5)$$

where  $\mathcal{F}\{\cdot\}$  and  $\mathcal{F}^{-1}\{\cdot\}$  correspond to the Fast Fourier Transform (FFT) and Inverse FFT (IFFT), respectively, and where  $u(n)$  is defined as:

$$u(n) = \begin{cases} 1, & n = 0, \frac{N}{2} \\ 2, & n = 1, 2, \dots, \frac{N}{2} - 1 \\ 0, & n = \frac{N}{2} - 1, \dots, N - 1 \end{cases} \quad (6)$$

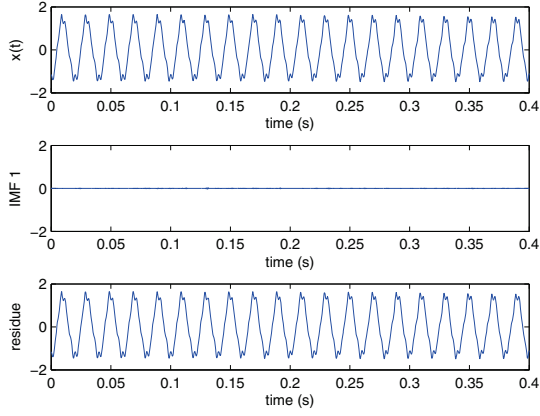


Fig. 3. EMD: Healthy generator (load 100W).

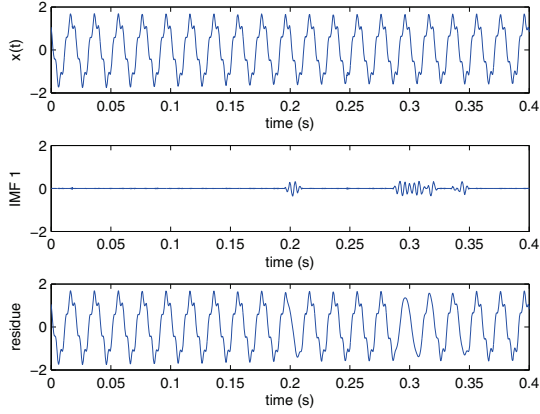


Fig. 4. EMD: Bearing inner race deterioration (load 100W).

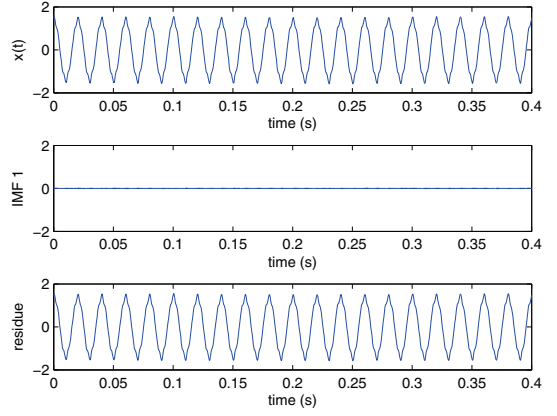


Fig. 5. EMD: Healthy generator (load 300W)

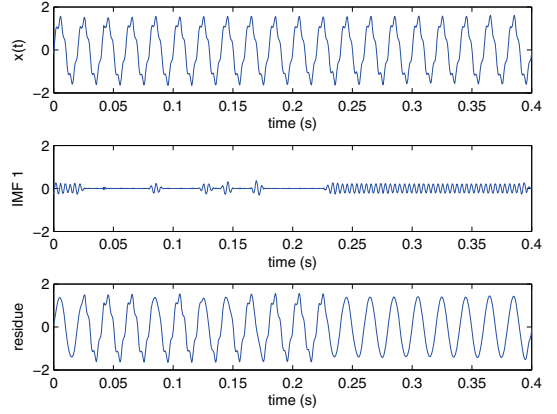


Fig. 6. EMD: Bearing ball deterioration (load 300W).

The estimated envelope, denoted  $|\hat{a}_1(n)|$ , is then given by [21]

$$|\hat{a}_1(n)| = \sqrt{y^2(n) + (\mathcal{H}[y(n)])^2} \quad (7)$$

Figures 7 to 10 display the amplitude envelope  $|\hat{a}_1(n)|$  for healthy and faulty generators. For healthy generators in Figs. 7 and 9, one can notice that the envelopes are close to 0 and do not exhibit strong variation. On the contrary, for faulty generators in Figs. 8 and 10, one can observe that the amplitude envelopes is no longer equal to 0 and exhibit much more variation.

### C. Failure Detection Criterion

In this section, we propose a simple criterion to distinguish between healthy and faulty generators. Let us consider the mono-component signal  $y(n)$  in (4). Without any failure, there is no amplitude modulation and so  $|\hat{a}_1(n)|$  is approximatively constant. When a failure occurs, the envelope  $|\hat{a}_1(n)|$  is no longer constant and exhibits variation. One measure of the amount of variation is the variance which is defined as

$$\sigma^2 = \frac{1}{N} \sum_{n=0}^{N-1} (|\hat{a}_1(n)| - \mu)^2 \quad (8)$$

where  $\mu$  is the average of  $|\hat{a}_1(n)|$ , i.e.

$$\mu = \frac{1}{N} \sum_{n=0}^{N-1} |\hat{a}_1(n)| \quad (9)$$

For healthy generator,  $|\hat{a}_1(n)|$  is supposed to be constant and so  $\sigma^2 = 0$ . On the contrary, for faulty generators,  $|\hat{a}_1(n)|$  exhibits variation and so  $\sigma^2 > 0$ . Therefore, the value of the statistical criterion  $\sigma^2$  can be used to distinguish between healthy and faulty generators. One should note that the coefficient  $N$  determines the compromise between robustness and reactivity of the criterion  $\sigma^2$ . Indeed, for a large  $N$ ,  $\sigma^2$  is less sensible to noise but it requires to analyse more data, which can increase latency of the diagnosis system.

## III. EXPERIMENTAL RESULTS

In this section, the result of the proposed approach is presented with experimental signals. Figure 11 describes the experimental setup that is operated in the motor configuration for experimental easiness. It is composed of two parts: a mechanical part that has a tacho-generator, a three-phase induction motor and an alternator. The tacho-generator is a

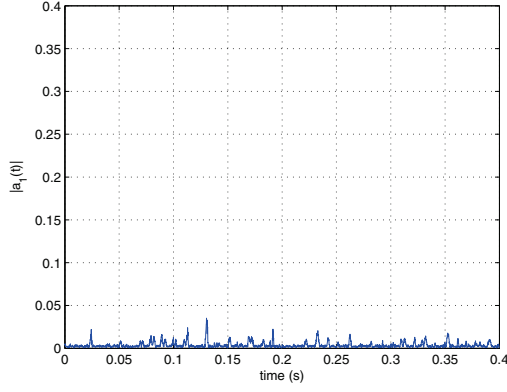


Fig. 7. AM demodulation: Healthy generator (load 100W).

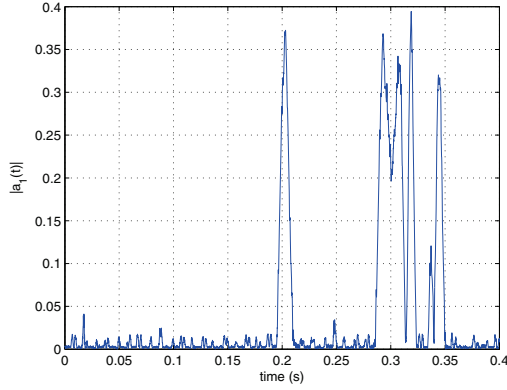


Fig. 8. AM demodulation: Bearing inner race deterioration (load 100W).

DC machine that generates 90 V at 3000 rpm. It is used to measure the speed. It produces linear voltage between 2500 and 3000 rpm. The alternator is a three-phase synchronous machine with a regulator and a rectifier circuit that stabilize the output voltage at 12 VDC. The advantage of using a car alternator instead of DC generator is obtaining constant output voltage at various speeds. The induction motor could be identically loaded at different speeds. Moreover, if the induction motor is supplied from the network, motor current will have time harmonic components as well as bearing fault harmonics. This makes it harder to determine the bearing failure effect on the stator current and therefore complicates the fault detection process. For these reasons, the induction motor is fed by an alternator. By this way, supply harmonics effects are eliminated and only bearing failure effects could be observed on the stator current.

The tested induction motor has the following rated parameters: 0.75kW, 220/380V, 1.95/3.4 A, 2780rpm, 50Hz, 2 poles, Y-connected. It has two 6204.2ZR type bearings. From the bearing data sheet the following parameters are obtained: The outside diameter is 47 mm and inside one is 20mm. Assuming that the inner and the outer races have the same thickness gives the pitch diameter  $D_P = 31.85\text{mm}$ . The bearing has eight balls ( $N = 8$ ) with an approximate diameter of  $D_B = 12\text{mm}$

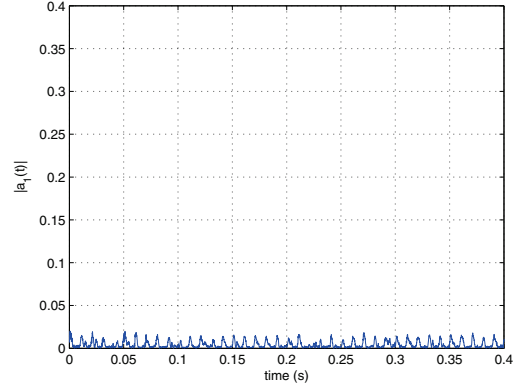


Fig. 9. AM demodulation: Healthy generator (load 300W).

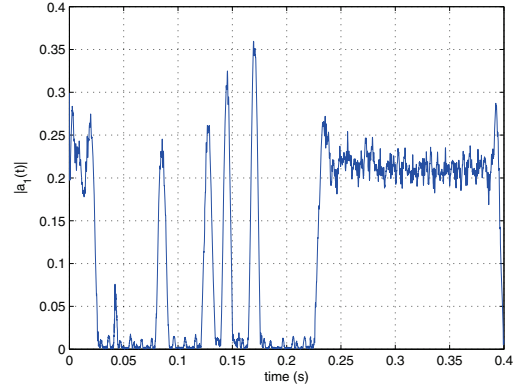


Fig. 10. AM demodulation: Bearing ball deterioration (load 300W).

TABLE I  
VALUES OF THE PROPOSED CRITERION  $\sigma^2$  FOR HEALTHY AND FAULTY GENERATORS (LOAD 100 W).

| Generator \ Signal       | $x(n)$               | $y(n) = \text{IMF}_1(n)$ |
|--------------------------|----------------------|--------------------------|
| Healthy generator        | $\sigma^2 = 0.02527$ | $\sigma^2 = 0.00020$     |
| Inner race deterioration | $\sigma^2 = 0.05036$ | $\sigma^2 = 0.00766$     |
| Cage deterioration       | $\sigma^2 = 0.05840$ | $\sigma^2 = 0.01156$     |
| Ball deterioration       | $\sigma^2 = 0.05517$ | $\sigma^2 = 0.00933$     |

TABLE II  
VALUES OF THE PROPOSED CRITERION  $\sigma^2$  FOR HEALTHY AND FAULTY GENERATORS (LOAD 200 W).

| Generator \ Signal       | $x(n)$               | $y(n) = \text{IMF}_1(n)$ |
|--------------------------|----------------------|--------------------------|
| Healthy generator        | $\sigma^2 = 0.01953$ | $\sigma^2 = 0.00012$     |
| Inner race deterioration | $\sigma^2 = 0.03893$ | $\sigma^2 = 0.00642$     |
| Cage deterioration       | $\sigma^2 = 0.04627$ | $\sigma^2 = 0.00231$     |
| Ball deterioration       | $\sigma^2 = 0.04652$ | $\sigma^2 = 0.01138$     |

and a contact angle  $\theta = 0^\circ$ . These bearings are made to fail by drilling holes of various radiuses with a diamond twist bit while controlling temperature by oil circulation in experiments. Some of the artificially deteriorated bearings are shown in Fig. 12.

Tables I, II and III present the value of the failure detection



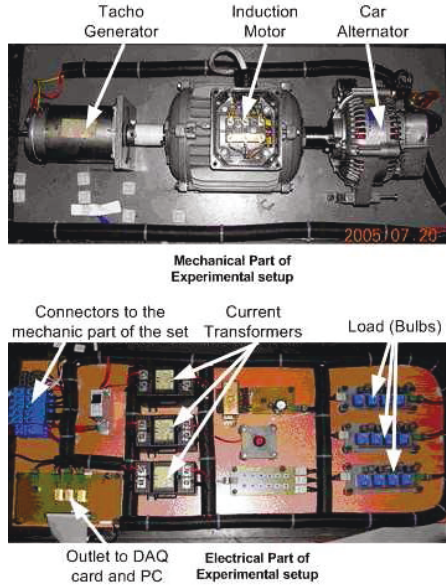


Fig. 11. Experimental setup [22].

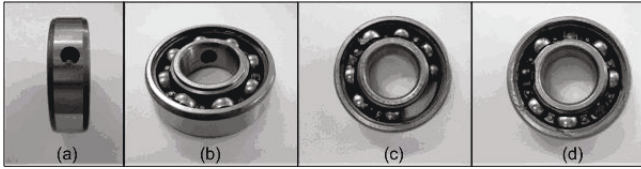


Fig. 12. Artificially deteriorated bearings: (a) outer race deterioration, (b) inner race deterioration, (c) cage deterioration, (d) ball deterioration [22].

TABLE III  
VALUES OF THE PROPOSED CRITERION  $\sigma^2$  FOR HEALTHY AND FAULTY GENERATORS (LOAD 300 W).

| Generator \ Signal       | $x(n)$               | $y(n) = \text{IMF}_1(n)$ |
|--------------------------|----------------------|--------------------------|
| Healthy generator        | $\sigma^2 = 0.01612$ | $\sigma^2 = 0.00001$     |
| Inner race deterioration | $\sigma^2 = 0.03457$ | $\sigma^2 = 0.00468$     |
| Cage deterioration       | $\sigma^2 = 0.03197$ | $\sigma^2 = 0.00210$     |
| Ball deterioration       | $\sigma^2 = 0.03324$ | $\sigma^2 = 0.01113$     |

criterion  $\sigma^2$  for several generator configurations. Let us denote  $x[n]$  the current signal. To highlight the use of the EMD preprocessing, the value of  $\sigma^2$  is also presented when the amplitude demodulation in (7) is performed on the signal current  $x(n)$ , directly, instead of on the first IMF  $y(n)$ . The three tables show that criterion  $\sigma^2$  is a good generator failure indicator which can be employed to detect several bearing failures (including inner race deterioration, cage deterioration and ball deterioration). Indeed, in each table,  $\sigma^2$  increases for faulty generators. Furthermore, the experimental results indicate that the proposed method works well under varying load conditions (100W, 200W and 300W). Compared to the direct application of amplitude-demodulation technique, the three tables also show that the use of the first Intrinsic Mode Function makes the failure detection easier. For example in table III, a ball deterioration leads to an increase of 106% when

the amplitude demodulation is performed on  $x(n)$  whereas it leads to an increase of 11120% when it is performed on  $y(n)$ . This result is not surprising since the stator current signal  $x(n)$  is usually multi-components in practice and so the amplitude demodulation cannot be extracted directly from  $x(n)$ . This explains why  $\sigma^2 \neq 0$  for healthy generator when it is computed from  $x(n)$ . On the contrary, the EMD preprocessing guarantees that the extracted IMF  $y(n)$  is a mono-component signal. Then, this signal can be further processed using an amplitude demodulation technique.

#### IV. CONCLUSION

The study reported in this paper focused on the bearing fault detection in DFIG-based wind turbine. Bearing failure is detected using current analysis. First, a mono-component signal is extracted from the stator current signal using an Empirical Mode Decomposition (EMD). Then, the first Intrinsic Mode Function is analyzed through amplitude-demodulation. The experimental results show that the proposed method works well under different conditions and can be applied for the detection of several bearing failures. Moreover, results show that the EMD preprocessing makes the failure detection easier as compared to the direct use of an amplitude demodulation technique.

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